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# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

**NATIONAL  
SENIOR CERTIFICATE/  
NASIONALE  
SENIOR SERTIFIKAAT**

**GRADE/GRAAD 12**

**MATHEMATICS P2/WISKUNDE V2**

**NOVEMBER 2019**

**MARKING GUIDELINES/NASIENRIGLYNE**

**MARKS/PUNTE: 150**

**These marking guidelines consist of 26pages.  
*Hierdie nasienriglyne bestaan uit 26 bladsye.***

**NOTE:**

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**NOTA:**

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.
- Om antwoorde/waardes te aanvaar om 'n probleem op te los, word NIE toegelaat NIE.

<b>GEOMETRY • MEETKUNDE</b>	
<b>S</b>	<b>A mark for a correct statement</b> (A statement mark is independent of a reason)
	<i>'n Punt vir 'n korrekte bewering</i> ( <i>'n Punt vir 'n bewering is onafhanklik van die rede</i> )
<b>R</b>	<b>A mark for the correct reason</b> (A reason mark may only be awarded if the statement is correct)
	<i>'n Punt vir 'n korrekte rede</i> ( <i>'n Punt word slegs vir die rede toegeken as die bewering korrek is</i> )
<b>S/R</b>	<b>Award a mark if statement AND reason are both correct</b>
	<i>Ken 'n punt toe as die bewering EN rede beide korrek is</i>

**QUESTION/VRAAG 1**

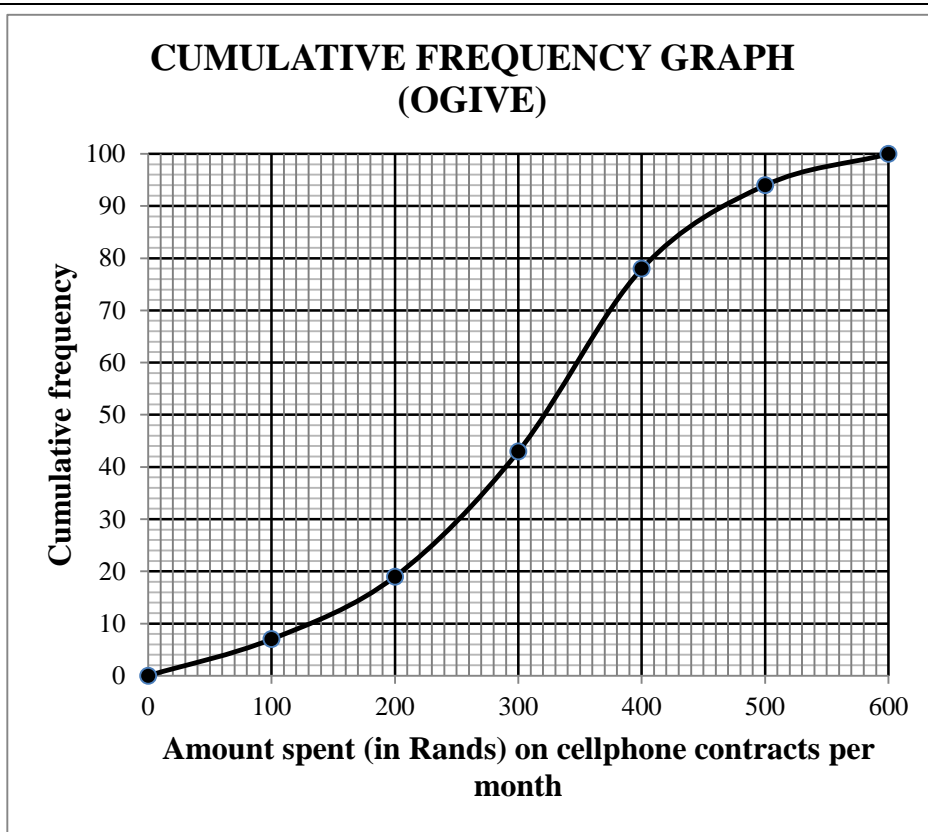
<b>Monthly income (in rands)</b> <b>Maandelikse inkomste (in rand)</b>	9 000	13 500	15 000	16 500	17 000	20 000
<b>Monthly repayment (in rands)</b> <b>Maandelikse paalement (in rand)</b>	2 000	3 000	3 500	5 200	5 500	6 000

1.1	$a = -1946,875... = -1946,88$ $b = 0,41$ $\hat{y} = -1946,88 + 0,41x$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div>	✓ $a = -1946,88$ ✓ $b = 0,41$ ✓ equation (3)
1.2	Monthly repayment $\approx$ R3 727,16 (calculator) <i>Maandelikse paalement <math>\approx</math> R3 727,16</i>  <b>OR</b>  $\hat{y} = -1946,88 + 0,41(14000)$ $\approx$ R3 793,12	✓✓ answer (2)  ✓ substitution ✓ answer (2)
1.3	$r = 0,946 \dots \approx 0,95$	✓ answer (1)
1.4	Not to spend R9 000 per month because the point (18 000 ; 9 000) lies very far from the least squares regression line. <b>OR D</b> <i>Spandeer nie R9 000 per maand nie, want die punt (18 000 ; 9 000) lê baie ver van die kleinste-kwadrate regressielyn. <b>OF D</b></i>	✓✓ answer (2)
<b>[8]</b>		

**QUESTION/VRAAG 2**

2.1	Number people paid R200 or less = 19 <i>Aantal mense wat R200 of minder betaal het = 19</i>	✓ answer (1)
2.2	$7 + 12 + a + 35 + b + 6 = 100$ $a = 40 - b$  $309 = \frac{(50 \times 7) + (150 \times 12) + (250 \times a) + (350 \times 35) + (450 \times b) + (550 \times 6)}{100}$ $309 = \frac{(50 \times 7) + (150 \times 12) + (250 \times (40 - b)) + (350 \times 35) + (450 \times b) + (550 \times 6)}{100}$ $350 + 1800 + 10000 - 250b + 12250 + 450b + 3300 = 30900$ $200b = 3200$ $b = 16$ $a = 24$  <b>OR/OF</b>  $7 + 12 + a + 35 + b + 6 = 100$ $b = 40 - a$  $309 = \frac{(50 \times 7) + (150 \times 12) + (250 \times a) + (350 \times 35) + (450 \times b) + (550 \times 6)}{100}$ $309 = \frac{(50 \times 7) + (150 \times 12) + (250 \times a) + (350 \times 35) + (450 \times (40 - a)) + (550 \times 6)}{100}$ $350 + 1800 + 250a + 12250 + 1800 - 450a = 30900$ $200a = 4\ 800$ $a = 24$ $b = 16$	✓ $\sum x = 100$ ✓ $a = 40 - b$  ✓ $\sum fX$ ✓ $\sum \frac{fX}{n} = 309$  ✓ $200b = 3200$  (5)  ✓ $\sum x = 100$ ✓ $b = 40 - a$  ✓ $\sum fX$ ✓ $\sum \frac{fX}{n} = 309$  ✓ $200a = 4\ 800$  (5)
2.3	Modal class/modale klas: $300 < x \leq 400$	✓ answer (1)

2.4



- ✓ grounded at (0 ; 0)
- ✓ (600 ; 100)
- ✓ cumulative frequencies for y-coordinates
- ✓ smooth shape

(4)

2.5

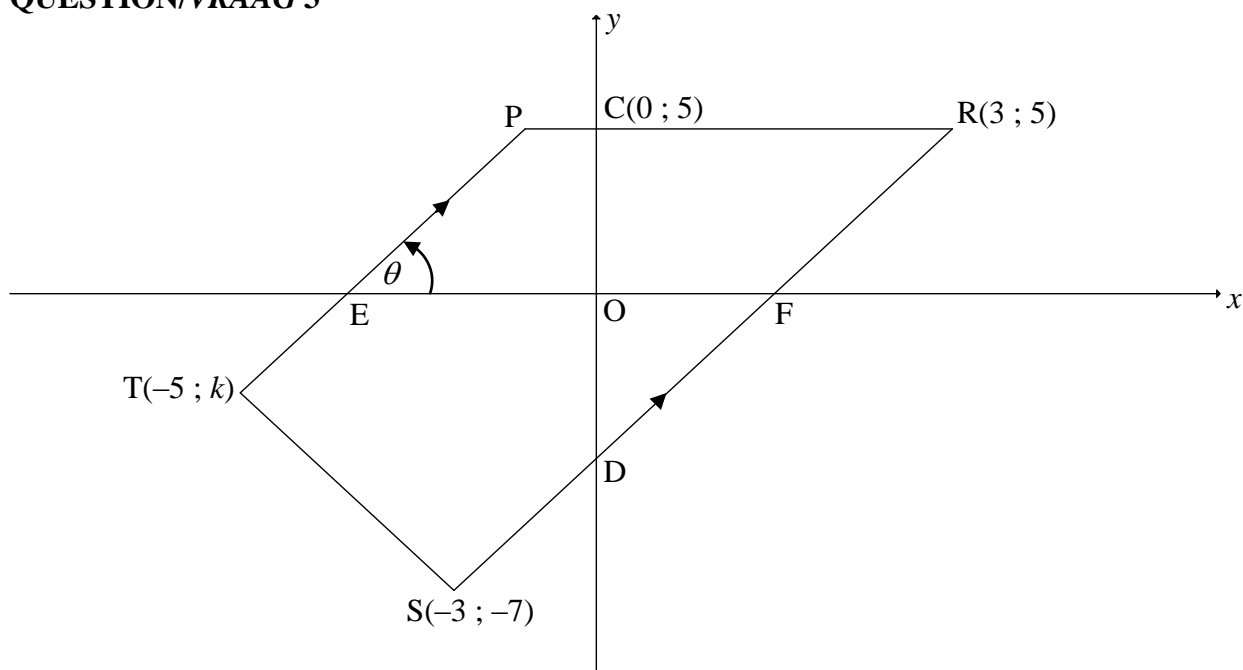
Number of people/Aantal mense =  $100 - 82$  [accept 80 – 84 people]  
 18 people paid more than R420 per month/. [accept 16 – 20 people]  
*18 mense betaal meer as R420 per maand*

Answer only: Full marks

- ✓ 82
- ✓ answer

(2)

**[13]**

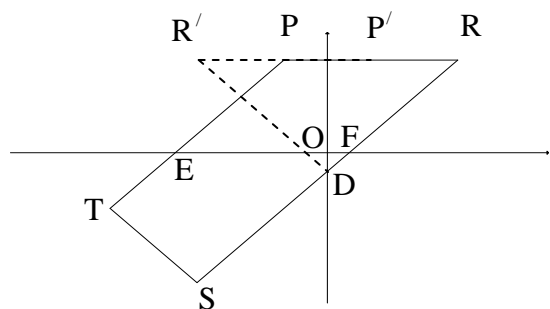
**QUESTION/VRAAG 3**

3.1	Equation of PR: $y = 5$	✓ answer (1)
3.2.1	$m_{RS} = \frac{y_2 - y_1}{x_2 - x_1}$ $m_{RS} = \frac{5 - (-7)}{3 - (-3)} = \frac{12}{6}$ $= 2$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: Full marks</div>	✓ substitution of R & S into gradient formula ✓ answer (2)
3.2.2	$m_{RS} = m_{PT}$ [PT $\parallel$ RS] $\tan \theta = 2$ $\theta = 63,43^\circ$	✓ $m_{RS} = m_{PT}$ ✓ $\tan \theta = 2$ ✓ $\theta = 63,43^\circ$ (3)
3.2.3	Equation of RS: $y - 5 = 2(x - 3)$ or $y - (-7) = 2(x - (-3))$ or $5 = 2(3) + c$ $y - 5 = 2x - 6$ $y + 7 = 2x + 6$ $c = -1$ $y = 2x - 1$ $y = 2x - 1$ $y = 2x - 1$ $\therefore D(0; -1)$  <b>OR/OF</b> $m_{RS} = m_{RD} = m_{DS}$ $2 = \frac{5 - y}{3 - 0} = \frac{y + 7}{0 - (-3)}$ $\therefore y = -1$ $\therefore D(0; -1)$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: Full marks</div>	✓ substitution ✓ equation of RS ✓ coordinates of D (3)  ✓ equating gradients ✓ value of y ✓ coordinates of D (3)

3.3	$ST = 2\sqrt{5} = \sqrt{[-5 - (-3)]^2 + (k - (-7))^2}$ $20 = 4 + (k + 7)^2$ $(k + 7)^2 = 16$ $k + 7 = \pm 4$ $k = -11 \text{ or } k = -3$ $\therefore k = -3$ <p><b>OR</b></p> $ST = 2\sqrt{5} = \sqrt{[-5 - (-3)]^2 + (k - (-7))^2}$ $20 = 4 + k^2 + 14k + 49$ $k^2 + 14k + 33 = 0$ $(k + 11)(k + 3) = 0$ $k = -11 \text{ or } k = -3$ $\therefore k = -3$	✓ substitute S and T into distance formula  ✓ isolate square ✓ square root both sides  ✓ answer (4)  ✓ substitute S and T into distance formula ✓ standard form ✓ factors  ✓ answer (4)
3.4	Method: translation $T \rightarrow S$ :  $(x; y) \rightarrow (x + 2; y - 4)$ $\therefore$ by symmetry: $D \rightarrow N$ : $D(0; -1) \rightarrow N(0 + 2; -1 - 4)$ $\therefore N(2; -5)$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div> <p><b>OR</b></p> Midpoint of TN = Midpoint of SD $\frac{x + (-5)}{2} = \frac{-3 + 0}{2} \text{ and } \frac{y + (-3)}{2} = \frac{-7 + (-1)}{2}$ $x = 2 \text{ and } y = -5$ $\therefore N(2; -5)$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div>	✓ method  ✓ x-coordinate ✓ y-coordinate (3)  ✓ method: midpoint of diagonals ✓ x-coordinate ✓ y-coordinate (3)



3.5



$\beta$  is the inclination of RS  $\therefore \beta = 63,434\dots^\circ$

$$\hat{O}FD = 63,434\dots^\circ \quad [\text{vert opp } \angle\text{s}]$$

$$\hat{O}DF = 90^\circ - 63,434\dots^\circ = 26,565\dots^\circ$$

$$\hat{R}DR' = 2(26,565\dots^\circ) = 53,13^\circ$$

**OR**

PEFR is a ||m [both pairs of opp sides ||]

$$\therefore \hat{R} = \theta = 63,434\dots^\circ \quad [\text{opp } \angle\text{s of ||m}]$$

$$\hat{R}R'D = 63,434\dots^\circ \quad [\angle\text{s opp = sides: } RD = R'D]$$

$$\hat{R}DR' = 180^\circ - (63,43^\circ + 63,43^\circ) [\text{sum of } \angle\text{s in } \Delta]$$

$$\hat{R}DR' = 53,13^\circ$$

**OR**

$$\tan \hat{O}DF = \frac{3}{6}$$

$$\hat{O}DF = 26,565\dots^\circ$$

$$\hat{R}DR' = 2(26,565\dots^\circ) = 53,13^\circ$$

**OR**

$R'(-3; 5)$  [reflection of  $R(3; 5)$  about the y-axis]

$$RD = \sqrt{(3-0)^2 + (5-(-1))^2}$$

$$RD = \sqrt{45} = R'D \quad \text{or} \quad 3\sqrt{5} \quad \text{or} \quad 6,71$$

$$(RR')^2 = (\sqrt{45})^2 + (\sqrt{45})^2 - 2(\sqrt{45})(\sqrt{45})(\cos \hat{R}DR')$$

$$6^2 = 45 + 45 - 2(45)(\cos \hat{R}DR')$$

$$\cos \hat{R}DR' = \frac{45 + 45 - 36}{2(45)}$$

$$\cos \hat{R}DR' = \frac{3}{5}$$

$$\therefore \hat{R}DR' = 53,13^\circ$$

$$\checkmark \beta = 63,43^\circ$$

$$\checkmark \hat{O}DF = 26,57^\circ$$

✓ answer

(3)

$$\checkmark \hat{R} = 63,43^\circ$$

$$\checkmark \hat{R}R'D = 63,43^\circ$$

✓ answer

(3)

✓ trig ratio

$$\checkmark \hat{O}DF = 26,565\dots^\circ$$

✓ answer

(3)

$$\checkmark R'(-3; 5) \quad \text{OR}$$

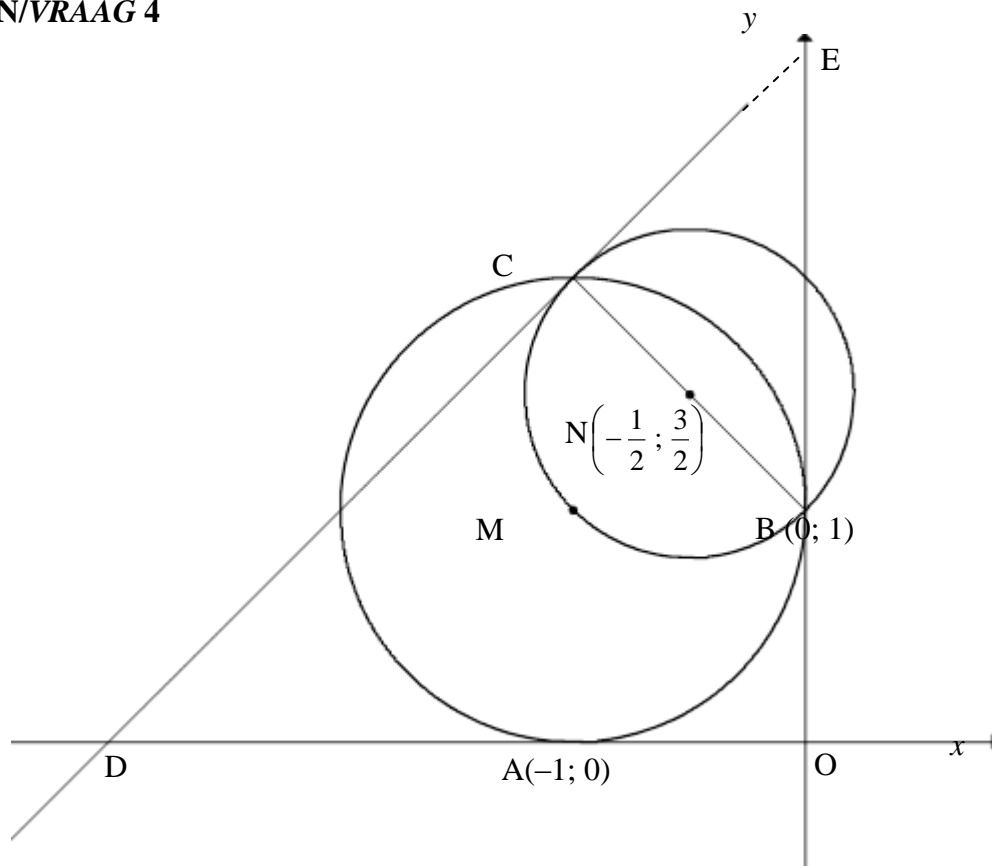
$$RD = \sqrt{45} = R'D$$

✓ substitution into cosine rule

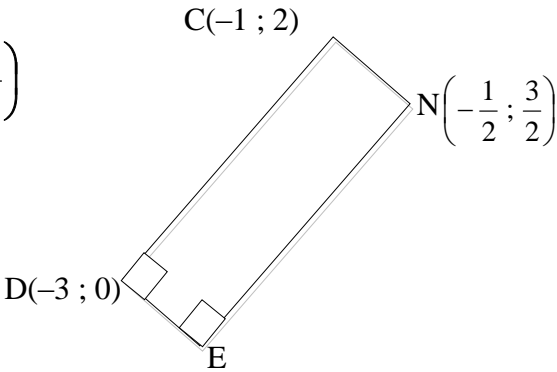
✓ answer

(3)

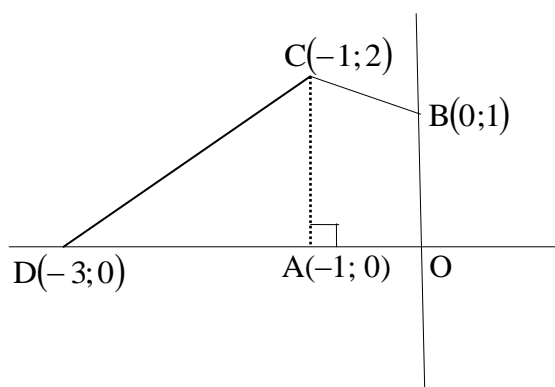
**[19]**

**QUESTION/VRAAG 4**

4.1	$M(-1; 1)$ $(x+1)^2 + (y-1)^2 = 1$	Answer only: Full marks	$\checkmark M(-1; 1)$ $\checkmark \text{LHS } \checkmark \text{RHS}$ (3)
4.2	Midpoint of CB, $N: (-0,5; 1,5)$ $\therefore \frac{x_C + 0}{2} = -\frac{1}{2}$ and $\frac{y_C + 1}{2} = \frac{3}{2}$ $\therefore C(-1; 2)$  <b>OR</b> $B \rightarrow N:$ $(x; y) \rightarrow (x - 0,5; y + 0,5)$ $N \rightarrow C:$ $(x; y) \rightarrow (x - 0,5; y + 0,5)$ $\therefore C(-0,5 - 0,5; 1,5 + 0,5)$ $\therefore C(-1; 2)$	Answer only: Full marks  Answer only: Full marks	$\checkmark x \text{ value } \checkmark y \text{ value}$ (2)  $\checkmark x \text{ value } \checkmark y \text{ value}$ (2)

4.3	$m_{\text{radius}} = \frac{2-1}{-1-0} \text{ OR } \frac{2-(-\frac{1}{2})}{-1-\frac{3}{2}} \text{ OR } \frac{0-(-\frac{1}{2})}{1-\frac{3}{2}}$ $= -1$ $\therefore m_{\text{tangent}} = 1$ $y = mx + c$ $y = x + c$ $2 = 1(-1) + c$ $c = 3$ $\therefore y = x + 3$ $y - x = 3$ <p><b>OR</b></p> $m_{\text{radius}} = \frac{2-1}{-1-0}$ $= -1$ $\therefore m_{\text{tangent}} = 1$ $y - y_1 = m(x - x_1)$ $y - y_1 = 1(x - x_1)$ $y - 2 = 1(x - (-1))$ $y - 2 = x + 1$ $\therefore y = x + 3$ $y - x = 3$	$\checkmark m_{\text{radius}}$ $\checkmark m_{\text{tangent}}$  $\checkmark$ substitute $(-1; 2)$ and $m$ $\checkmark$ simplification (4)  $\checkmark m_{\text{radius}}$ $\checkmark m_{\text{tangent}}$  $\checkmark$ substitute $(-1; 2)$ and $m$ $\checkmark$ simplification (4)
4.4	Tangents to circle: $y = x + 3$ and $y = x + 1$  $\therefore t > 3$ or $t < 1$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answers only: Full marks</div>	$\checkmark y = x + 1$  $\checkmark t > 3$ $\checkmark t < 1$ (3)
4.5	Draw rectangle CNED:  Midpt of DN $\left(-\frac{7}{4}; \frac{3}{4}\right)$ $\therefore E(-\frac{5}{2}; -\frac{1}{2})$   <p><b>OR/OF</b></p> $D(-3; 0)$ $C \rightarrow N:$ $(x; y) \rightarrow (x + 0,5; y + 0,5)$ $D \rightarrow E:$ $D(x; y) \rightarrow E(x + 0,5; y + 0,5)$ $\therefore E(-3 + 0,5; 0 + 0,5)$ $\therefore E(-2,5; 0,5)$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: Full marks</div>	$\checkmark$ midpt of DN  $\checkmark x$ value $\checkmark y$ value (3)  $\checkmark$ coordinates of D  $\checkmark x$ value $\checkmark y$ value (3)

4.6



$$\begin{aligned}\text{area of trapezium AOBC} &= \frac{1}{2}(1+2)(1) \\ &= 1\frac{1}{2} \text{ square units}\end{aligned}$$

$$\begin{aligned}\text{area of } \triangle ACD &= \frac{1}{2}(2)(2) \\ &= 2 \text{ square units}\end{aligned}$$

$$\text{area of quadrilateral OBCD} = 3\frac{1}{2} \text{ square units}$$

$$\begin{aligned}\therefore 2a^2 &= \frac{7}{2} \\ a^2 &= \frac{7}{4} \\ a &= \frac{\sqrt{7}}{2}\end{aligned}$$

**OR**

✓ substitution into area of trapezium form

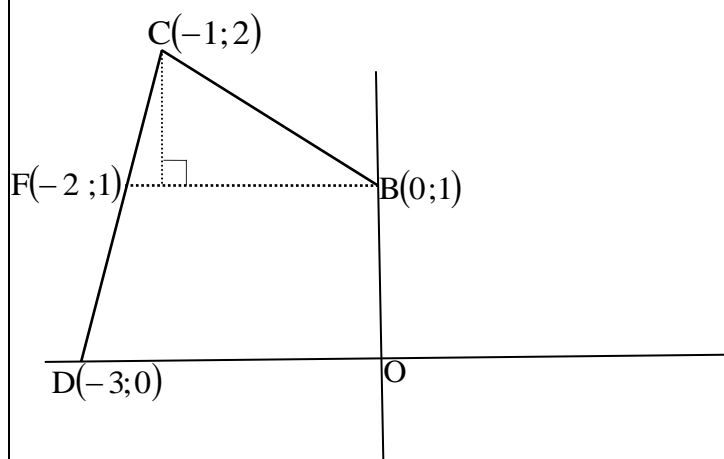
✓ area of trapezium

✓ area of triangle

✓ area of OBCD

✓ equating area OBCD to  $2a^2$ 

(5)



BM produced cuts the tangent at F.

$$\text{area of } \triangle CFB = \frac{1}{2}(2)(1)$$

$$= 1 \text{ square unit}$$

$$\text{area of trapezium BFDO} = \frac{1}{2}(2+3)(1)$$

$$= 2\frac{1}{2} \text{ square units}$$

$$\text{area of quadrilateral OBCD} = 3\frac{1}{2} \text{ square units}$$

$$\therefore 2a^2 = \frac{7}{2}$$

$$a^2 = \frac{7}{4}$$

$$a = \frac{\sqrt{7}}{2}$$

**OR**

✓ area of triangle

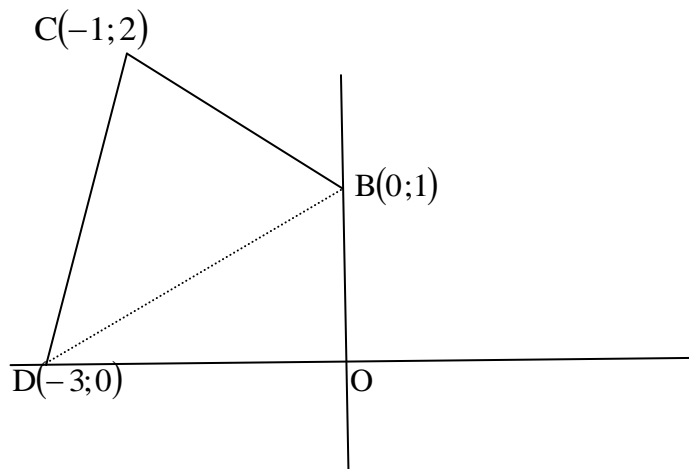
✓ substitution into  
area of trapezium

✓ area of trapezium

✓ area of OBCD

✓ equating area  
OBCD to  $2a^2$

(5)



Join DB

$$\begin{aligned}\text{area of } \triangle ODB &= \frac{1}{2}(3)(1) \\ &= \frac{3}{2} \text{ square unit}\end{aligned}$$

$$\begin{aligned}\text{area of } \triangle DCB &= \frac{1}{2}(2\sqrt{2})(\sqrt{2}) \\ &= 2 \text{ square unit}\end{aligned}$$

$$\therefore \text{area of OBCD} = \frac{3}{2} + 2 = \text{square units}$$

$$2a^2 = \frac{7}{2}$$

$$a^2 = \frac{7}{4}$$

$$a = \frac{\sqrt{7}}{2}$$

**OR**

✓ area of  $\Delta$

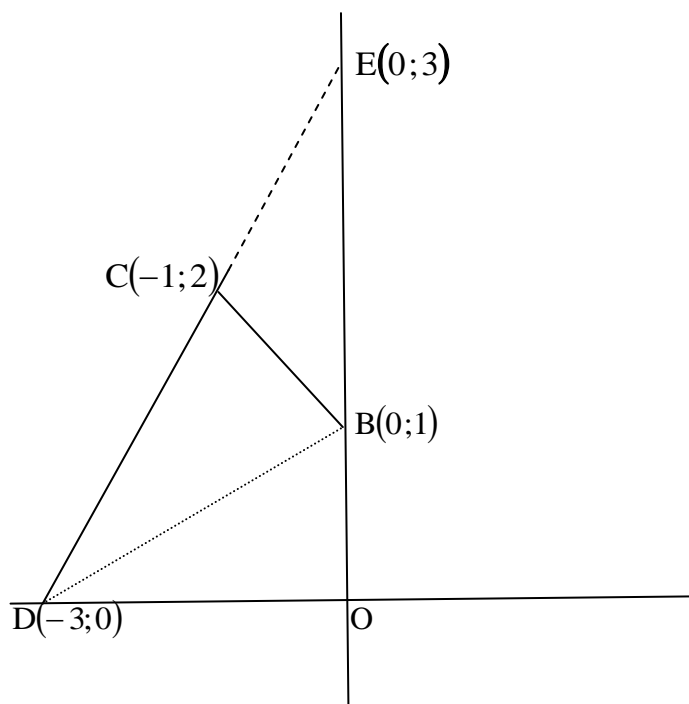
✓ subst into area of  $\Delta$

✓ area of  $\Delta$

✓ area of OBCD

✓ equating area  
OBCD to  $2a^2$

(5)



Let E be the point of intersection of DC with the positive y-axis.

$$\text{area of } \triangle DEO = \frac{1}{2}(3)(3)$$

$$= \frac{9}{2} \text{ square unit}$$

$$\text{area of } \triangle ECB = \frac{1}{2}(2)(1) \text{ or } \frac{1}{2}(\sqrt{2})(\sqrt{2})$$

$$= 1 \text{ square unit}$$

$$\text{area of quadrilateral OBCD} = \frac{9}{2} - 1 = 3\frac{1}{2} \text{ square units}$$

$$\therefore 2a^2 = \frac{7}{2}$$

$$a^2 = \frac{7}{4}$$

$$a = \frac{\sqrt{7}}{2}$$

✓ area of  $\Delta$

✓ subst into area of  $\Delta$

✓ area of  $\Delta$

✓ area of OBCD

✓ equating area  
OBCD to  $2a^2$

(5)

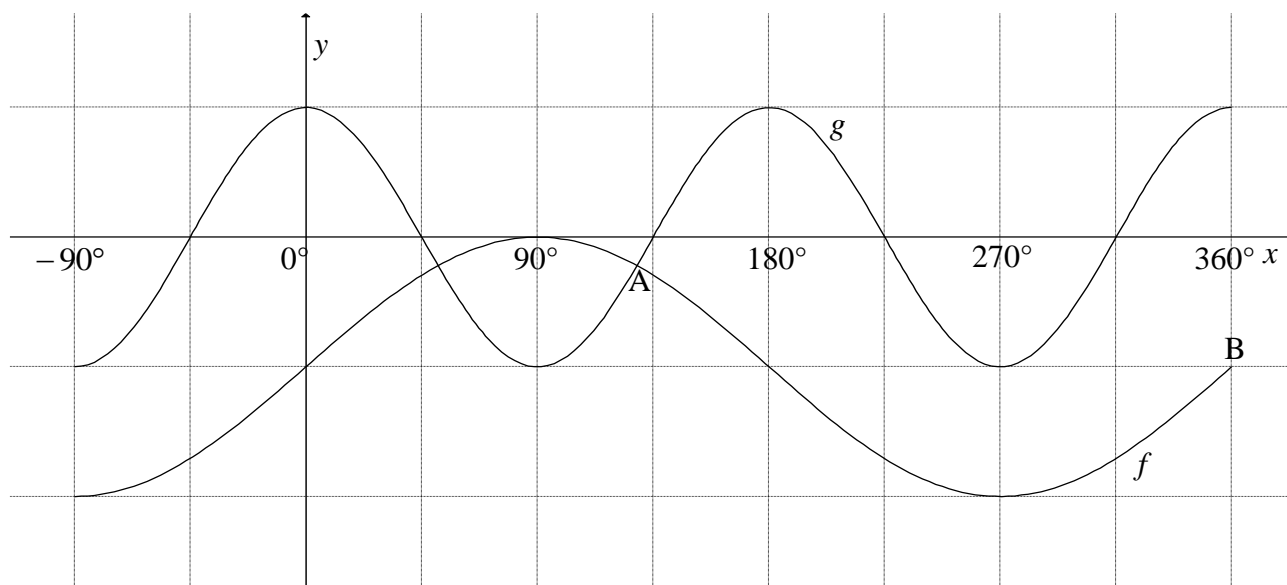
[20]

**QUESTION/VRAAG 5**

5.1	$\frac{\sin x}{\cos x \cdot \tan x} + \sin(180^\circ + x) \cos(90^\circ - x)$ $= \frac{\sin x}{\cos x \cdot \frac{\sin x}{\cos x}} + (-\sin x) \sin x$ $= 1 - \sin^2 x$ $= \cos^2 x$	$\checkmark -\sin x$ $\checkmark \sin x$ $\checkmark \tan x = \frac{\sin x}{\cos x}$ $\checkmark 1 - \sin^2 x$ $\checkmark \cos^2 x$ (5)
5.2	$\frac{\sin^2 35^\circ - \cos^2 35^\circ}{4 \sin 10^\circ \cos 10^\circ}$ $= \frac{-(\cos^2 35^\circ - \sin^2 35^\circ)}{2(2 \sin 10^\circ \cos 10^\circ)}$ $= \frac{-\cos 70^\circ}{2 \sin 20^\circ}$ $= \frac{-\cos 70^\circ}{2 \cos 70^\circ} \quad \text{OR} \quad = \frac{-\sin 20^\circ}{2 \sin 20^\circ} = -\frac{1}{2}$	$\checkmark -(\cos^2 35^\circ - \sin^2 35^\circ)$ $\checkmark -\cos 70^\circ$ $\checkmark 2 \sin 20^\circ$  $\checkmark \text{answer}$ (4)
5.3	$2 \sin^2 77^\circ = 2[\sin(90^\circ - 13^\circ)]^2$ $= 2 \cos^2 13^\circ$ $= 2 \cos^2 13^\circ - 1 + 1$ $= \cos 26^\circ + 1$ $= m + 1$ <b>OR</b> $1 - 2 \sin^2 77^\circ = \cos 154^\circ$ $2 \sin^2 77^\circ = 1 - \cos 154^\circ$ $= 1 - (-\cos 26^\circ)$ $= 1 + m$	$\checkmark$ using co-ratio $\checkmark$ reduction  $\checkmark 2 \cos^2 13^\circ - 1 = \cos 26^\circ$ $\checkmark \text{answer}$ (4) $\checkmark 1 - 2 \sin^2 77^\circ = \cos 154^\circ$ $\checkmark 2 \sin^2 77^\circ = 1 - \cos 154^\circ$ $\checkmark$ reduction $\checkmark \text{answer}$ (4)
5.4.1	$\sin(x + 25^\circ) \cos 15^\circ - \cos(x + 25^\circ) \sin 15^\circ = \tan 165^\circ$ $\sin(x + 25^\circ - 15^\circ) = -0,2679... \text{ OR } -2 + \sqrt{3}$ $\sin(x + 10^\circ) = -0,2679... \text{ OR } -2 + \sqrt{3}$ $x + 10^\circ = 195,54^\circ + k \cdot 360^\circ \quad \text{or} \quad x + 10^\circ = 344,46^\circ + k \cdot 360^\circ$ $x = 185,54^\circ + k \cdot 360^\circ; k \in \mathbb{Z} \quad \text{or} \quad x = 334,46^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ <b>OR/OF</b>	$\checkmark \checkmark \sin(x + 10^\circ)$ $\checkmark -0,2679...$ $\checkmark 195,54^\circ \text{ \& } 344,46^\circ$ $\checkmark 185,54^\circ \text{ \& } 334,46^\circ$ $\checkmark + k \cdot 360^\circ; k \in \mathbb{Z}$ (6)

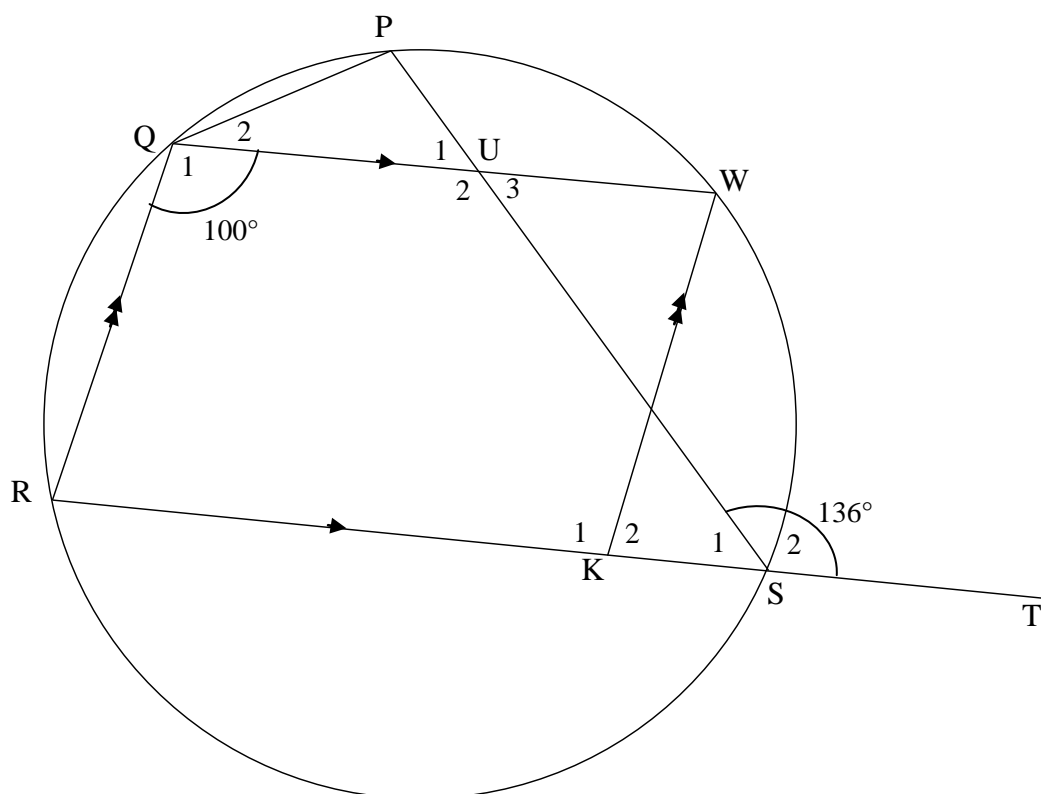


	$\sin(x + 25^\circ)\sin 75^\circ - \cos(x + 25^\circ)\cos 75^\circ = \tan 165^\circ$ $-(\cos(x + 25^\circ)\cos 75^\circ - \sin(x + 25^\circ)\sin 75^\circ) = -0,2679...$ $\cos(x + 100^\circ) = 0,2679...$ $\text{ref. } \angle = 74.4577...^\circ$ $x + 100^\circ = 74,46^\circ + k.360^\circ \text{ or } x + 100^\circ = 285,54^\circ + k.360^\circ$ $x = -25,54^\circ + k.360^\circ; k \in \mathbb{Z} \text{ or } x = 185,54^\circ + k.360^\circ; k \in \mathbb{Z}$	$\checkmark \checkmark \cos(x + 100^\circ)$ $\checkmark -0,2679...$  $\checkmark 74,46^\circ \text{ \& } 285,54^\circ$ $\checkmark -25,54^\circ \text{ \& } 185,54^\circ$ $\checkmark + k.360^\circ; k \in \mathbb{Z}$ (6)
5.4.2	$f(x) = \sin(x + 10^\circ)$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answers only: Full marks</div> For minimum value of $\sin x$ : $x = 270^\circ$ For minimum value of $\sin(x + 10^\circ)$ : $x = 260^\circ$	$\checkmark f(x) = \sin(x + 10^\circ)$  $\checkmark 270^\circ$ $\checkmark \text{ answer}$ (3)
		[22]

**QUESTION/VRAAG 6**

6.1	Range of $f$ : $y \in [-2; 0]$ <b>OR</b> $-2 \leq y \leq 0$	✓ critical values ✓ notation (2)
6.2	$x \in (90^\circ; 270^\circ)$ OR $x \in [90^\circ; 270^\circ]$	✓ critical values ✓ notation (2)
6.3	$PQ = \cos 2x - (\sin x - 1)$ $= 1 - 2\sin^2 x - \sin x + 1$ $= -2\sin^2 x - \sin x + 2$ $\sin x = -\frac{b}{2a}$ $= \frac{-(-1)}{2(-2)}$ $\sin x = -\frac{1}{4}$ $\therefore x = 194,48^\circ$ or $x = 345,52^\circ$	✓ $PQ = \cos 2x - (\sin x - 1)$ ✓ $\cos 2x = 1 - 2\sin^2 x$  ✓ substitution into formula  ✓ $\sin x = -\frac{1}{4}$ ✓ $194,48^\circ$ ✓ $345,52^\circ$ (6)
<b>[10]</b>		

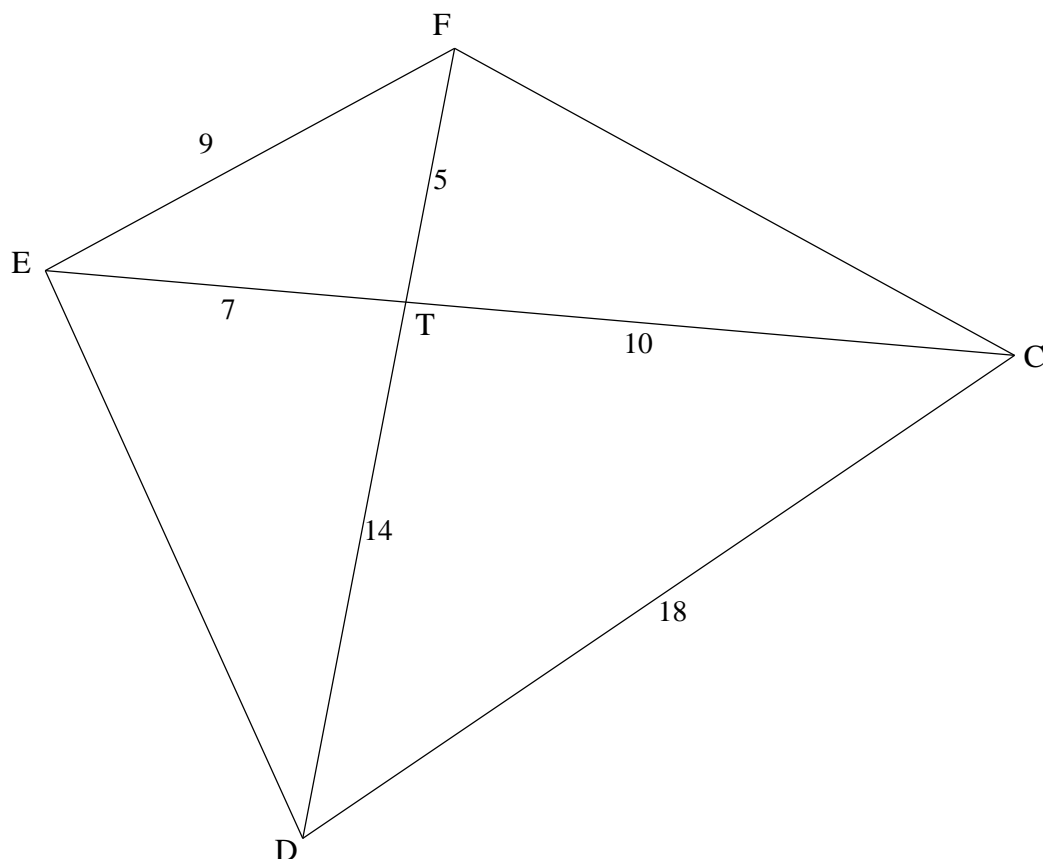


**QUESTION/VRAAG 8**

8.1.1	$\hat{R} = 80^\circ$ [co-int $\angle$ s/ko-binne $\angle$ e; $QW \parallel RK$ ]	✓S ✓R (2)
8.1.2	$\hat{P} = 100^\circ$ [opp $\angle$ s of cyclic quad/teenoorst $\angle$ e v koordevh ]	✓S ✓R (2)
8.1.3	<p><math>\hat{PQR} = 136^\circ</math> [ext <math>\angle</math> of cyclic quad/buite <math>\angle</math> v koordevh]</p> <p><math>\hat{Q}_2 = 36^\circ</math></p> <p><b>OR</b></p> <p><math>\hat{PUW} = \hat{S}_2 = 136^\circ</math> [corresp <math>\angle</math>s/ooreenkomstige <math>\angle</math>e; <math>QW \parallel RK</math>]</p> <p><math>\hat{PQW} + \hat{P} = \hat{PUW}</math> [ext <math>\angle</math>s of/buite <math>\angle</math> van <math>\Delta QPU</math>]</p> <p><math>\hat{PQW} + 100^\circ = 136^\circ</math></p> <p><math>\hat{PQW} = 36^\circ</math></p> <p><b>OR</b></p> <p><math>\hat{U}_3 = 180^\circ - 136^\circ = 44^\circ</math> [co-int <math>\angle</math>s/ko-binne <math>\angle</math>e; <math>QW \parallel RK</math>]</p> <p><math>\hat{U}_1 = \hat{U}_3 = 44^\circ</math> [vert opp <math>\angle</math>s/regoorstaande <math>\angle</math>e ]</p> <p><math>\hat{PQW} = 180^\circ - (100 + 44^\circ)</math> [sum of <math>\angle</math>s in <math>\Delta</math>/som <math>\angle</math>e van <math>\Delta</math>]</p> <p><math>\hat{PQW} = 36^\circ</math></p>	<p>✓S ✓R ✓S (3)</p> <p>✓S ✓R  ✓S (3)</p> <p>✓S ✓R   ✓S (3)</p>



8.2



8.2.1	<p>In <math>\triangle EFT</math> and <math>\triangle DCT</math>:</p> $\frac{EF}{CD} = \frac{9}{18} = \frac{1}{2}$ $\frac{FT}{TC} = \frac{5}{10} = \frac{1}{2}$ $\frac{ET}{TD} = \frac{7}{14} = \frac{1}{2}$ <p><math>\therefore \triangle EFT \parallel \triangle DCT</math> [ Sides of <math>\Delta</math> in prop/ sye van <math>\Delta</math> in dieselfde verh ]</p> <p><math>\therefore \hat{EFD} = \hat{ECD}</math></p> <p><b>OR</b></p> <p>In <math>\triangle FET</math>:</p> $49 = 25 + 81 - 2(5)(9)\cos\hat{F}$ $\cos\hat{F} = \frac{19}{30}$ $\hat{F} = 50,7^\circ$ <p>In <math>\triangle TDC</math>:</p> $196 = 100 + 256 - 2(10)(18)\cos\hat{C}$ $\cos\hat{C} = \frac{19}{30}$ $\hat{C} = 50,7^\circ$	<p>✓✓ all 3 ratios = <math>\frac{1}{2}</math></p> <p>✓ <math>\triangle EFT \parallel \triangle DCT</math> ✓ R</p> <p>(4)</p> <p>✓✓ <math>\hat{F} = 50,7^\circ</math></p> <p>✓✓ <math>\hat{C} = 50,7^\circ</math></p> <p>(4)</p>
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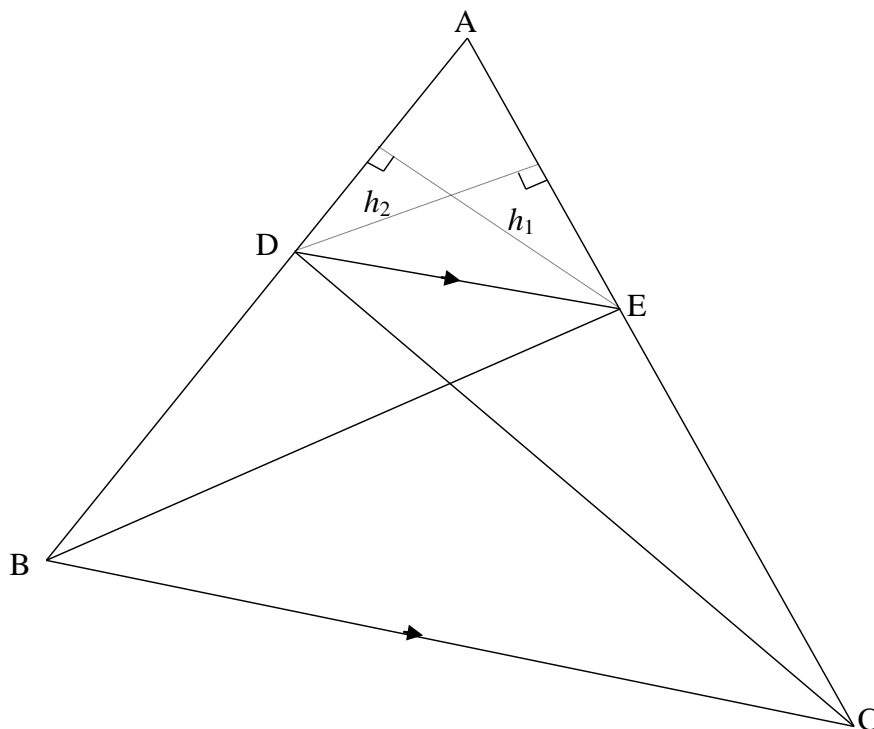
8.2.2	$\hat{E}FD = \hat{E}CD$ [proved in 8.2.1] E, F, C and D are concyclic EFCD is a cyclic quad [converse $\angle$ s in the same segment/ <i>omgekeerde <math>\angle</math>e in dies segment</i> ] $\therefore \hat{D}FC = \hat{D}EC$ [ $\angle$ s in the same segment/ <i><math>\angle</math>e in dies segment</i> ]	✓S ✓R  ✓ R  (3)
<b>[16]</b>		





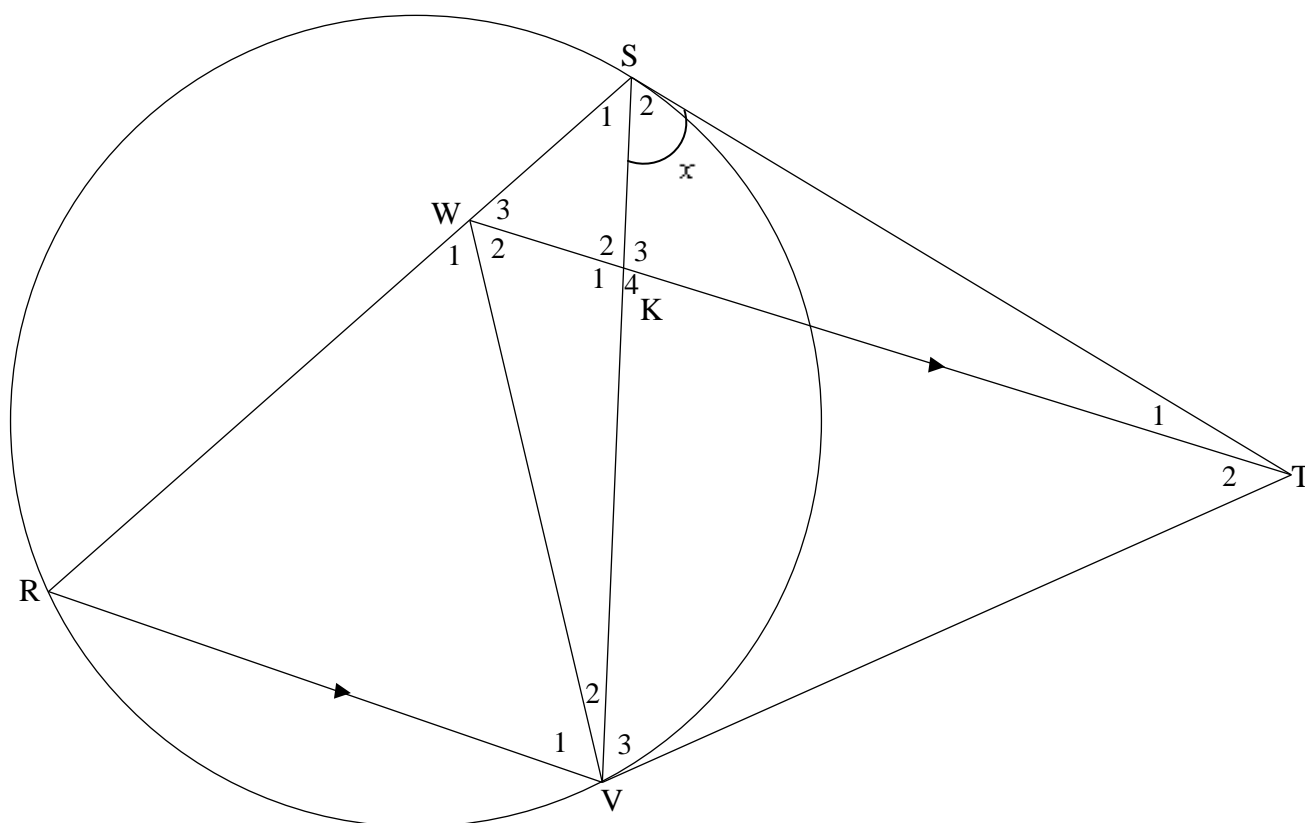
## QUESTION/VRAAG 10

10.1



10.1	<p>Constr: Draw <math>h_1</math> from <math>E \perp AD</math> and <math>h_2</math> from <math>D \perp AE</math>  Konstr: Trek <math>h_1</math> vanaf <math>E \perp AD</math> en <math>h_2</math> vanaf <math>D \perp AE</math></p> <p>Proof/Bewys:</p> $\frac{\text{area } \triangle ADE}{\text{area } \triangle BDE} = \frac{\frac{1}{2} AD \times h_1}{\frac{1}{2} DB \times h_1} = \frac{AD}{DB}$ $\frac{\text{area } \triangle ADE}{\text{area } \triangle DEC} = \frac{\frac{1}{2} AE \times h_2}{\frac{1}{2} EC \times h_2} = \frac{AE}{EC}$ <p>But area <math>\triangle BDE</math> = area <math>\triangle DEC</math> [same base &amp; height or <math>DE \parallel BC</math>/  dies basis &amp; hoogte; of <math>DE \parallel BC</math>]</p> $\therefore \frac{\text{area } \triangle ADE}{\text{area } \triangle BDE} = \frac{\text{area } \triangle ADE}{\text{area } \triangle DEC}$ $\therefore \frac{AD}{DB} = \frac{AE}{EC}$	<p>✓ constr/konstr <b>OR</b>  reason: common  vertex or  same height</p> $\checkmark \frac{\text{area } \triangle ADE}{\text{area } \triangle BDE} = \frac{\frac{1}{2} AD \times h_1}{\frac{1}{2} DB \times h_1}$ $\checkmark \frac{\text{area } \triangle ADE}{\text{area } \triangle DEC} = \frac{AE}{EC}$ <p>✓ S ✓ R  ✓ S</p> <p>(6)</p>
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10.2



10.2.1	$\hat{V}_3 = x$ [Tans from same point/raaklyne vanaf dieselfde pt] $\hat{R} = x$ [tan chord theorem/raaklyn koordstelling] $\hat{W}_3 = x$ [corresp $\angle$ s/ooreenkomstige $\angle$ e; $WT \parallel RV$ ]	$\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ R $\checkmark$ S $\checkmark$ R	(6)
10.2.2(a)	$\hat{V}_3 = \hat{W}_3 = x$ [proved in 10.2.1] W, S, T and V are concyclic/is konsiklies WSTV is a cyclic quad [converse $\angle$ s in the same segment/ Omgekeerde $\angle$ e in dieselfde segment]	$\checkmark$ S $\checkmark$ R	(2)
10.2.2(b)	$\hat{W}_2 = \hat{S}_2 = x$ [ $\angle$ s in the same segment/ $\angle$ e in dies segment] $\hat{V}_1 = \hat{W}_2 = x$ [alt $\angle$ s/verwiss $\angle$ e ; $WT \parallel RV$ ] But $\hat{R} = x$ [proved in 10.2.1] $\therefore \hat{R} = \hat{V}_1 = x$ $\therefore WR = WV$ [sides opp equal $\angle$ s/sye teenoor gelyke $\angle$ e] $\Delta WRV$ is isosceles/is gelykbenig <b>OR/OF</b>	$\checkmark$ S $\checkmark$ R $\checkmark$ S/ R $\checkmark$ S	(4)

	$\hat{S}_2 = \hat{W}_2 = x$ [∠s in the same segment] $\hat{W}_2 = \hat{W}_3 = x$ $\hat{W}_2 + \hat{W}_3 = \hat{R} + \hat{V}_1$ [ext ∠ of Δ] $\therefore \hat{V}_1 = x = \hat{R}$ $\therefore WR = WV$ [sides opp equal ∠s/sye teenoor gelyke ∠e] ΔWRV is isosceles/is gelykbenig	✓ S ✓ R  ✓ S/ R ✓ S  (4)
10.2.2(c)	In ΔWRV and/en ΔTSV $\hat{R} = \hat{S}_2 = x$ [proved <b>OR</b> tan chord theorem] $\hat{V}_1 = \hat{V}_3 = x$ [proved] $\therefore \Delta WRV \parallel \Delta TSV$ [∠, ∠, ∠]  <b>OR/OF</b>  In ΔWRV and/en ΔTSV $\hat{R} = \hat{S}_2 = x$ [proved <b>OR</b> tan chord theorem] $\hat{V}_1 = \hat{V}_3 = x$ [proved] $\hat{W}_1 = \hat{S}TV = x$ [sum of ∠s in Δ/∠e van Δ] $\therefore \Delta WRV \parallel \Delta TSV$	✓ S  ✓ S ✓ R  (3)   ✓ S ✓ S ✓ S  (3)
10.2.2(d)	$\frac{RV}{SV} = \frac{WR}{TS}$ [ΔWRV ∥ ΔTSV] $\therefore WR \times SV = RV \times TS$ $\frac{WR}{SR} = \frac{KV}{SV}$ [prop theorem/eweredighst; WT ∥ RV] $\therefore WR \times SV = KV \times SR$ $\therefore RV \times TS = KV \times SR$ $\therefore \frac{RV}{SR} = \frac{KV}{TS}$  <b>OR/OF</b>  In ΔRVS and/en ΔVKT $\hat{S}VR = \hat{K}_4$ [alt ∠s, WT ∥ RV] $\hat{S}RV = \hat{V}_3$ [proven] ΔRVS ∥ ΔVKT [∠, ∠, ∠] $\therefore \frac{RV}{SR} = \frac{KV}{VT}$ but VT = ST [tans from same point] $\therefore \frac{RV}{SR} = \frac{KV}{TS}$	✓ correct ratios  ✓ $\frac{WR}{SR} = \frac{KV}{SV}$ ✓ R  ✓ equating $WR \times SV$  (4)   ✓ identifying correct Δs  ✓ proving ∥  ✓ correct ratio  ✓ S  (4)
<b>[25]</b>		

**TOTAL/TOTAAL: 150**